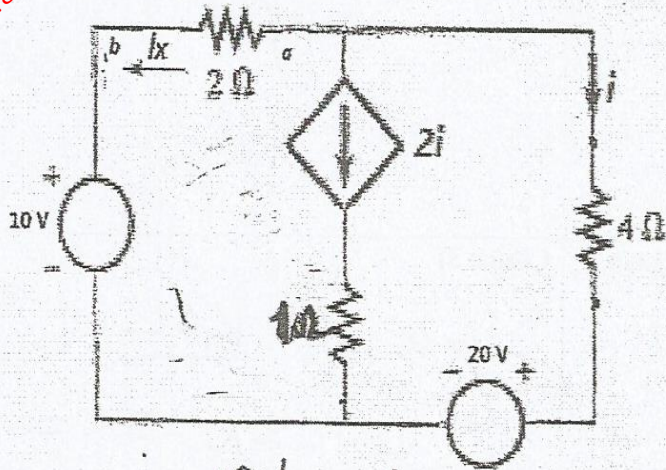
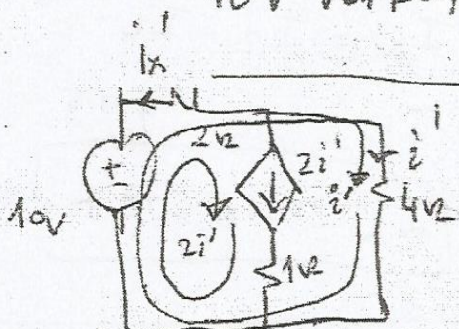


Soru 1) Şekilde verilen devrede a-b arasındaki $2\ \Omega$ 'luk direncin akımını (i_x) Süperpozisyon (toplamsallık) teoremini kullanarak bulunuz. (35 P)



10V voltaj (20V → K.D.)
 $2i$ devrede



i' için KVL

$$4 \cdot i' - 10 + 2 \cdot (i' + 2i') = 0$$

$$10i' = 10$$

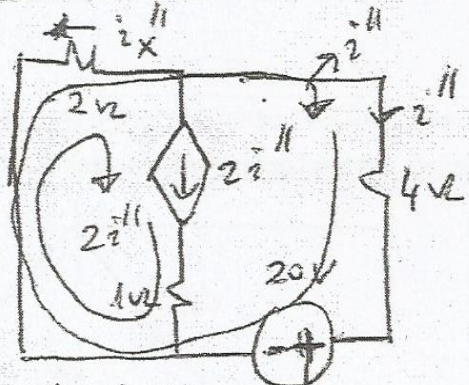
$$i' = 1A$$

$$i_x = -3i'$$

$$i_x' = -3A$$

Çözüm 1)

20 Voltaj
($2i$ devrede, 10V K.D.)



i'' için KVL

$$4 \cdot i'' + 20 + 2 \cdot (2i'' + i'') = 0$$

$$10i'' = -20$$

$$i'' = -2A$$

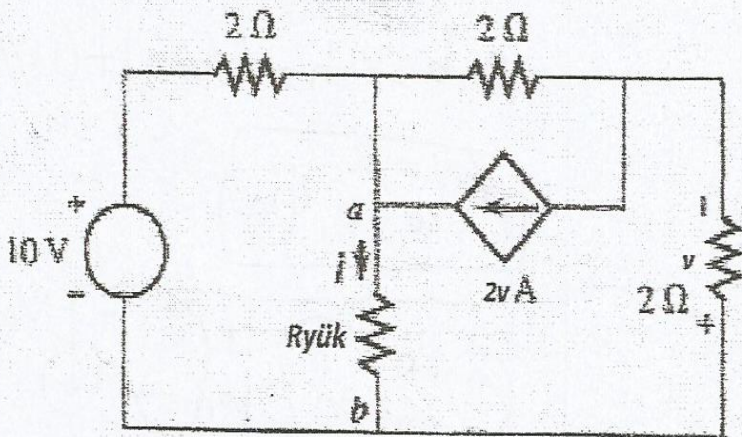
$$i_x'' = -3i'' = 6A$$

Sonuç olarak

$$i_x = i_x' + i_x''$$

$$i_x = -3 + 6 = 3A$$

Soru 2) Şekilde verilen devrede a-b arasındaki Ryük direncine iletebilecek maksimum gücü bulunuz. (35 P)



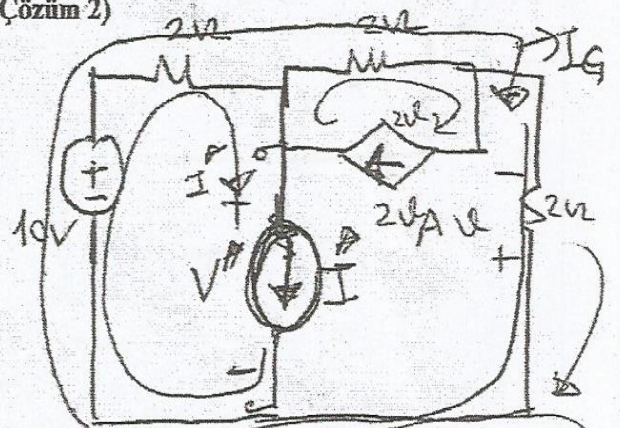
V^p için I^p gerisi → KVL

$$V^p - 10 + 2 \cdot (I^p + I) = 0$$

$$V^p - 10 + 2I^p + 2 \cdot (I^p - 5) = 0$$

$$V^p = 4(-I^p) + 20$$

Çözüm 2)



I_g için KVL

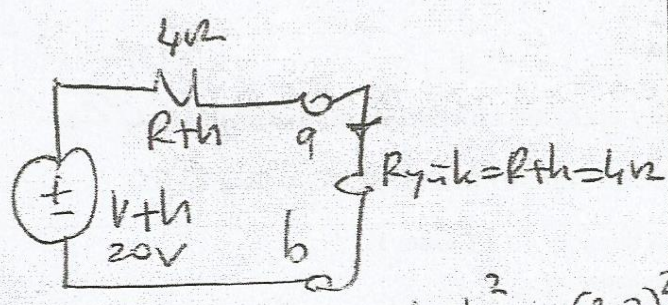
$$V = -2I_g$$

$$2V = -4I_g$$

$$-10 + 2 \cdot (I^p + I_g) + 2 \cdot (-4I_g + I_g)$$

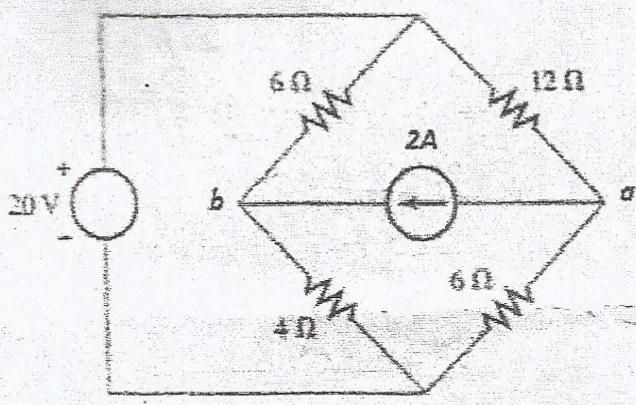
$$I_g(-6 + 2) + I^p(2) - 10 = 0$$

$$-2I_g = 10 - 2I^p$$



$$P_{max, R_{yük}} = \frac{V_{th}^2}{4R_{th}} = \frac{(20)^2}{4 \cdot 4} = \frac{20 \cdot 20}{4 \cdot 4} = 25 \text{ W}$$

Soru3) Şekilde verilen devrede, a-b arasındaki akım kaynağının gücünü, Norton Teoremi'ni kullanarak bulunuz. (30 P)



Cözüm 3)

a için KCL

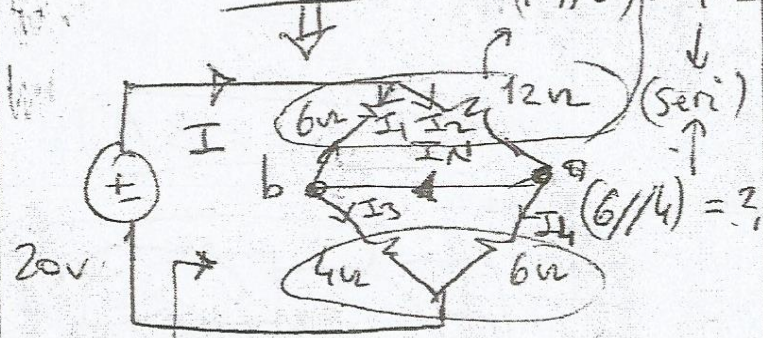
$$I_2 - I_N - I_4 = 0$$

$$I_N = I_2 - I_4$$

$$I_N = 1,041 - 1,25$$

$$I_N = -0,209 \text{ A}$$

I_N için



$$R_{eq} = 4 + 2,4 = 6,4 \Omega$$

$$I = \frac{20}{6,4} \text{ A} = 3,125 \text{ A}$$

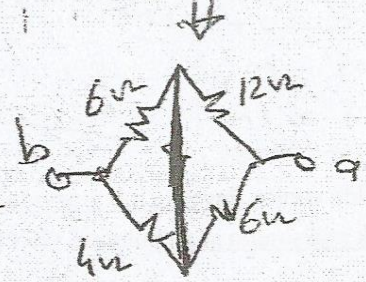
$$I_1 = 3,125 \cdot \frac{12}{18} \approx 2,083 \text{ A}$$

$$I_2 = 3,125 \cdot \frac{6}{18} \approx 1,041 \text{ A}$$

$$I_3 = 3,125 \cdot \frac{6}{10} = 1,875 \text{ A}$$

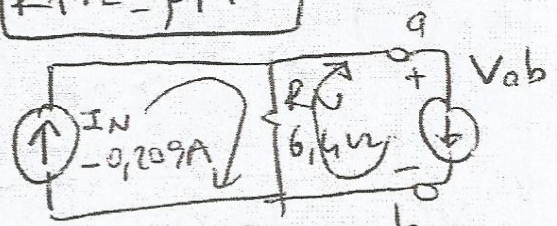
$$I_4 = 3,125 \cdot \frac{4}{10} = 1,25 \text{ A}$$

R_N



$$R_{ab} = R_{th} = (6//4) + (12//6)$$

$$R_{th} = 2,4 + 4 = 6,4 \Omega$$



$$V_{RN} = V_{ab} = 6,4 \cdot (-0,209 - 2)$$

Süre: 60 DK

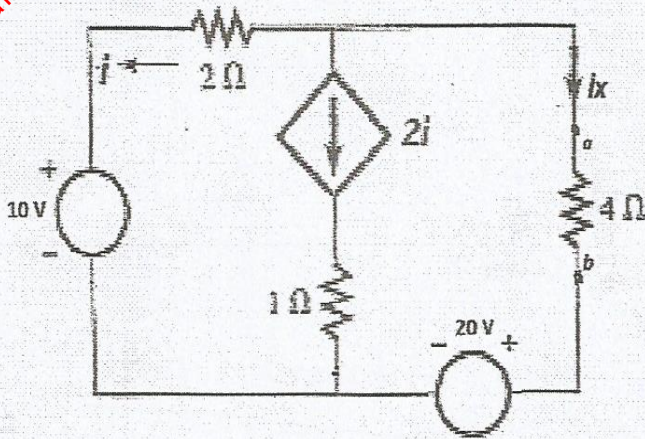
BAŞARILAR..

Doç.Dr. Ercan İZGİ

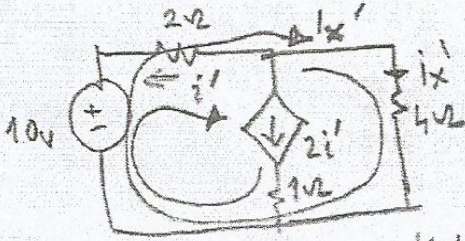
$$V_{ab} = 13,56 \text{ V}$$

$$P_{ab} = 2 \cdot (-13,56) = -27,12 \text{ W}$$

Soru 1) Şekilde verilen devrede a-b arasındaki 4 Ω'luk direncin akımını (i_x) Süperpozisyon (toplamsallık) teoremini kullanarak bulunuz. (35 P)



10 V varken ($2i$ devrede)



$$i' = -2i' - i_x'$$

$$3i' = -i_x'$$

$$i' = -\frac{1}{3}i_x'$$

i_x' için KVL

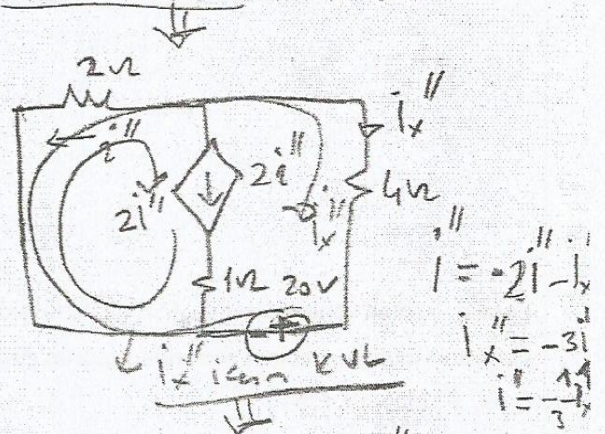
$$-10 + 2(i_x' + 2i') + 4i_x' = 0$$

$$-10 + 2(i_x' + 2(-\frac{1}{3}i_x')) + 4i_x' = 0$$

$$i_x'(2 - \frac{4}{3} + 4) = 10 \Rightarrow \frac{14}{3}i_x' = 10 \Rightarrow i_x' = \frac{15}{7}A$$

Çözüm 1)

20 V varken ($10V \rightarrow K-D$
 $2i \rightarrow devrede$)



$$i'' = -2i'' - i_x''$$

$$i_x'' = -3i''$$

$$i'' = -\frac{1}{3}i_x''$$

$$4 \cdot i_x'' + 2(i_x'' + 2i'') + 20 = 0$$

$$4 \cdot i_x'' + 2(i_x'' + 2(-\frac{1}{3}i_x'')) + 20 = 0$$

$$i_x''(4 + 2 - \frac{4}{3}) = -20$$

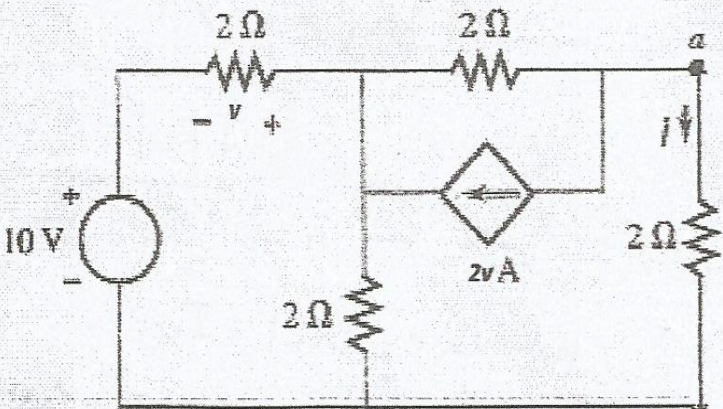
$$\frac{14}{3}i_x'' = -20$$

$$i_x'' = -\frac{30}{7}A$$

Sonuç olarak

$$i_x = i_x' + i_x'' = \frac{15}{7} - \frac{30}{7} = -\frac{15}{7}A$$

Soru 2) Şekilde verilen devrede a-b arasındaki 2Ω'luk direncin akımını Norton teoremini kullanarak bulunuz. (35 P)



$$E + 2I - 5 - I + 2I - 8(\frac{5}{2} + \frac{I}{2}) = 0$$

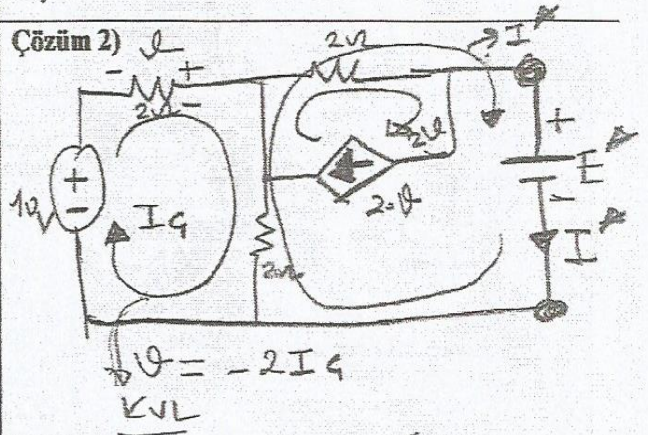
$$E + I(2 - 4 + 2) + (-5 - 20) = 0$$

$$-I + E - 25 = 0$$

$$-I = -E + 25$$

$$I = E - 25$$

Çözüm 2)



$$V = -2I_Q$$

KVL

$$-10 + 4I_Q - 2I = 0$$

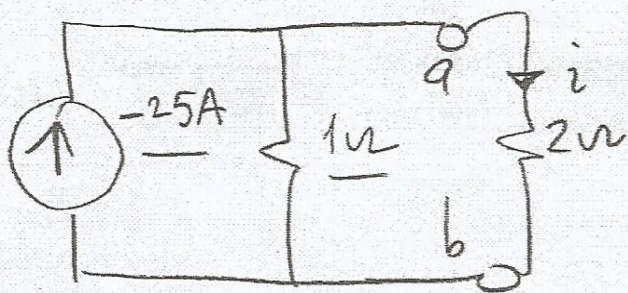
$$4I_Q - 2I + 10 = 0$$

$$I_Q = \frac{5}{2} + \frac{I}{2}$$

I için KVL

$$E + 2(I - I_Q) + 2(I + 2V) = 0$$

$$E + 2I - 2(\frac{5}{2} + \frac{I}{2}) + 2I + 4(-2I_Q) = 0$$



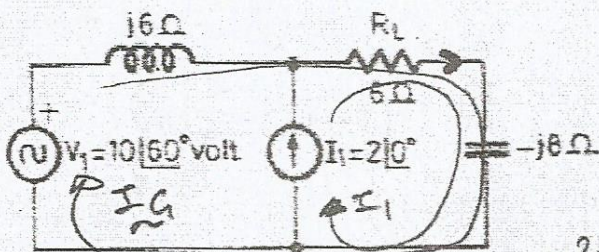
$$i = (-25) \cdot \frac{1}{1+2}$$

$$i = \frac{-25}{3} = -8,33 \text{ A}$$

Soru3) Şekilde verilen devrede, SSH'de (Sinüsoidal Sürekli Hal) R_L direncinin akımını, bobinin ve kondansatörün güçlerini ($Q_L = X_L \cdot i^2$, $Q_C = X_C \cdot i^2$) bulunuz. (30 P)

Çözüm 3)

(~) → fazörel ifret



→ 2∠0°

$$-V_1 + (j6) \cdot I_G + 6 \cdot (I_1 + I_G) - (j8) \cdot (I_1 + I_G) = 0$$

$$-10\angle 60^\circ + I_G(j6 + 6 - j8) + (12 - 16j) = 0$$

$$I_G(6 - 2j) = 10\angle 60^\circ + 16j - 12$$

$$I_G = \frac{10\angle 60^\circ + 16j - 12}{6 - 2j} = -2,28 + j3,35 \text{ A}$$

$$I_G \approx 4 \angle 124^\circ \text{ A}$$

$$I_{RL} = I_1 + I_G = 2\angle 0^\circ + 4\angle 124^\circ = 3,32 \angle 94^\circ$$

$$|I_{RL}| \approx 3,32 \text{ A}$$

$$P_{RL} = |R_L| |I_{RL}|^2 = 6 \cdot (3,32)^2 \approx 66 \text{ W}$$

$$Q_C = |X_C| \cdot (I_C)$$

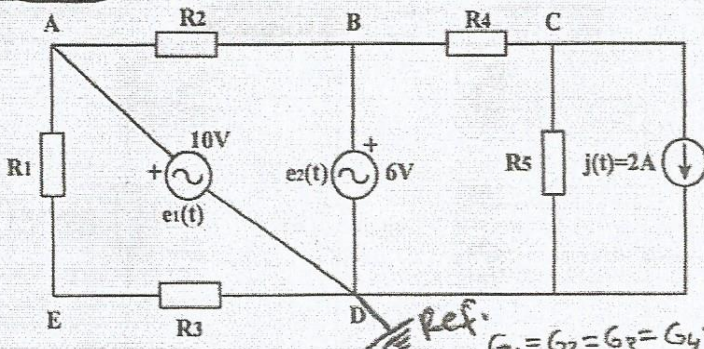
$$Q_C = (8) \cdot (3,32)^2 \approx 88 \text{ VAR}$$

$$Q_L = |X_L| |I_L|^2 = 6 \cdot (4)^2 = 96 \text{ VAR}$$

(+)

kap. (-)

SORU 1)



$V_A = e_1(t) = 10V$
 $V_B = e_2(t) = 6V$ } Biliniyor
 $V_C = ?$
 $V_E = ?$ } Bilinmiyor
 $V_D = 0 = \text{Referans Dügüm}$

Ref. $G_1 = G_2 = G_3 = G_4 = G_5 = 2 \text{ mhos}$

a)

$$\begin{bmatrix} G_4 + G_5 & 0 \\ 0 & G_1 + G_3 \end{bmatrix} \begin{bmatrix} V_C \\ V_E \end{bmatrix} + \begin{bmatrix} 0 & -G_4 \\ -G_1 & 0 \end{bmatrix} \begin{bmatrix} e_1(t) \\ e_2(t) \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} j(t) = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

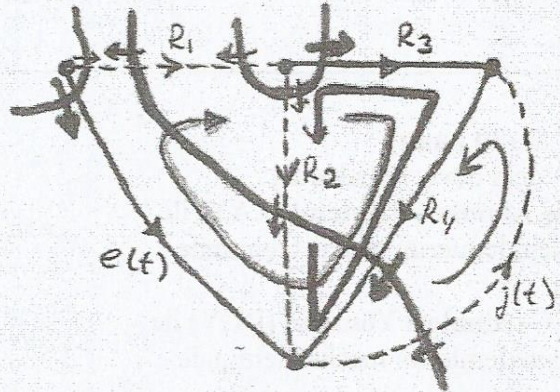
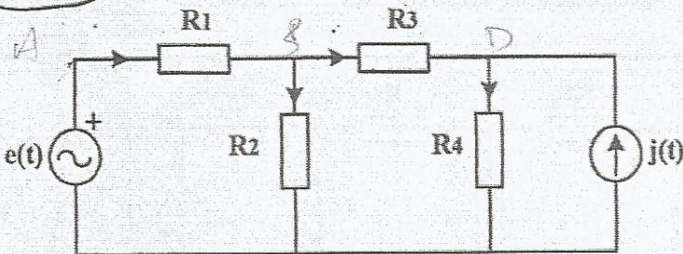
$$\begin{bmatrix} 4 & 0 \\ 0 & 4 \end{bmatrix} \begin{bmatrix} V_C \\ V_E \end{bmatrix} = \begin{bmatrix} 0 & 2 \\ 2 & 0 \end{bmatrix} \begin{bmatrix} e_1(t) \\ e_2(t) \end{bmatrix} + \begin{bmatrix} -1 \\ 0 \end{bmatrix} j(t)$$

$$\begin{bmatrix} 4V_C \\ 4V_E \end{bmatrix} = \begin{bmatrix} 0 & 2 \\ 2 & 0 \end{bmatrix} \begin{bmatrix} 10 \\ 6 \end{bmatrix} + \begin{bmatrix} -1 \\ 0 \end{bmatrix} 2 \Rightarrow \begin{bmatrix} 4V_C \\ 4V_E \end{bmatrix} = \begin{bmatrix} 10 \\ 20 \end{bmatrix} \Rightarrow \begin{matrix} V_C = 2,5V \\ V_E = 5V \end{matrix}$$

b) $i_{R4} = \frac{V_{R4}}{R_4} = \frac{V_B - V_C}{R_4} = \frac{6 - 2,5}{0,5} = 7A \Rightarrow P_{R4} = i_{R4}^2 \cdot R_4 = 24,5W$

$B \xrightarrow{i_{R4} = 7A} R_4 \xrightarrow{C} [B \rightarrow C \text{ yönünde}]$

SORU 3)



a) KAY ile

$$\begin{bmatrix} R_1 + R_3 + R_4 & -(R_3 + R_4) \\ -(R_3 + R_4) & R_2 + R_3 + R_4 \end{bmatrix} \begin{bmatrix} i_{R1} \\ i_{R2} \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \end{bmatrix} e(t) + \begin{bmatrix} -R_4 \\ R_4 \end{bmatrix} j(t)$$

b) DGY ile

$$\begin{bmatrix} G_1 + G_2 + G_3 & 0 \\ G_1 + G_2 & G_1 + G_2 + G_4 \end{bmatrix} \begin{bmatrix} V_{R3} \\ V_{R4} \end{bmatrix} = \begin{bmatrix} G_1 \\ G_1 \end{bmatrix} e(t) + \begin{bmatrix} 0 \\ 1 \end{bmatrix} j(t)$$

$\rightarrow a = -2$ $\rightarrow d = -3$ ($a \neq d$)

④ $\frac{d}{dt} i_L(t) = -2 i_L(t) + 3 - 4e^{-3t} + 2 \cos 2t$ $i_L(0) = 5A$

a) Ö2 çözüm, $i_{L_{\text{ö2}}}(t) = i_L(0) \cdot e^{at} \Rightarrow \boxed{i_{L_{\text{ö2}}}(t) = 5e^{-2t}}$

b) Özel çözüm, $\boxed{i_{L_{\text{özel}}}(t) = A + Be^{-3t} + C \cos 2t + D \sin 2t}$

Bu özel çözümün dif. denklemini sağlaması gerekir,

$\frac{d}{dt} i_{L_{\text{özel}}}(t) = -3Be^{-3t} - 2C \sin 2t + 2D \cos 2t$

$\frac{d}{dt} i_{L_{\text{özel}}}(t) = -2 i_{L_{\text{özel}}}(t) + 3 - 4e^{-3t} + 2 \cos 2t$

$-3Be^{-3t} - 2C \sin 2t + 2D \cos 2t = -2(A + Be^{-3t} + C \cos 2t + D \sin 2t) + 3 - 4e^{-3t} + 2 \cos 2t$

$-3Be^{-3t} - 2C \sin 2t + 2D \cos 2t = (3 - 2A) + (-2B - 4)e^{-3t} - 2D \sin 2t + (2 - 2C) \cos 2t$

$$\begin{cases} 3 - 2A = 0 \\ A = \frac{3}{2} \end{cases} \left\{ \begin{array}{l} -2C = -2D \\ C = D \end{array} \right. \left\{ \begin{array}{l} 2D = 2 - 2C \\ C = D \text{ idi} \\ 2C = 2 - 2C \\ 4C = 2 \end{array} \right. \left\{ \begin{array}{l} C = \frac{1}{2} \\ c = 0 \Rightarrow D = \frac{1}{2} \end{array} \right. \left\{ \begin{array}{l} -3B = -2B - 4 \\ B = 4 \end{array} \right.$$

$i_{L_{\text{özel}}}(t) = A + Be^{-3t} + C \cos 2t + D \sin 2t$

$\boxed{i_{L_{\text{özel}}}(t) = \frac{3}{2} + 4e^{-3t} + \frac{1}{2} \cos 2t + \frac{1}{2} \sin 2t}$

$i_{L_{\text{özel}}}(0) = \frac{3}{2} + 4e^0 + \frac{1}{2} \cos 0$

$\boxed{i_{L_{\text{özel}}}(0) = 6}$

Zorlanmış çözüm, $i_{L_{\text{zor}}}(t) = i_{L_{\text{özel}}}(t) - e^{at} i_{L_{\text{özel}}}(0)$

$\boxed{i_{L_{\text{zor}}}(t) = \frac{3}{2} + 4e^{-3t} + \frac{1}{2} \cos 2t + \frac{1}{2} \sin 2t - 6e^{-2t}}$

Tam çözüm: $i_{L_{\text{tam}}}(t) = i_{L_{\text{özel}}}(t) + i_{L_{\text{zor}}}(t)$

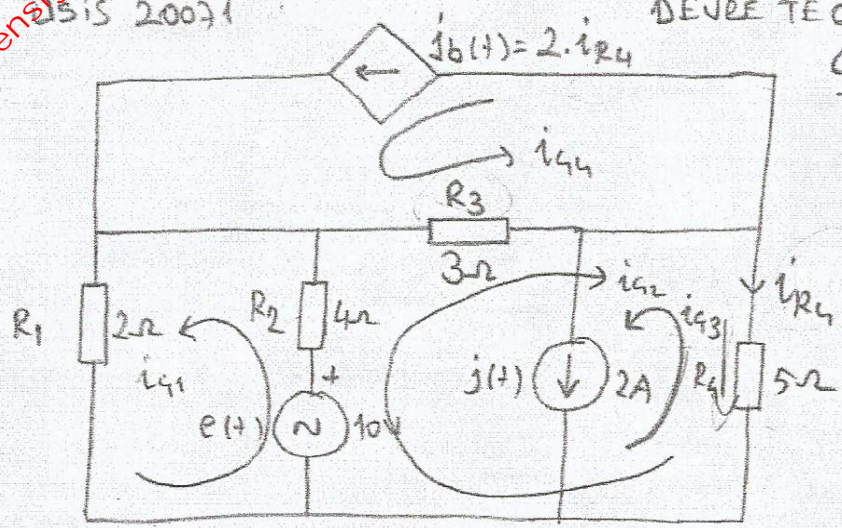
$i_{L_{\text{tam}}}(t) = 5e^{-2t} + \frac{3}{2} + 4e^{-3t} + \frac{1}{2} \cos 2t + \frac{1}{2} \sin 2t - 6e^{-2t}$

$\boxed{i_{L_{\text{tam}}}(t) = -e^{-2t} + \frac{3}{2} + 4e^{-3t} + \frac{1}{2} \cos 2t + \frac{1}{2} \sin 2t}$

Kontrol: $i_L(0) = -e^0 + \frac{3}{2} + 4e^0 + \frac{1}{2} \cos 0 + \frac{1}{2} \sin 0 = 5$ (doğru)

0515 20071

DEURE TEO. 1 VIZE SINAVI
CEVAP ANAHTARI



$i_{R1} = ?$
 $i_{R2} = ?$
 $i_{R3} = j(t) = 2A$
 $i_{R4} = j_b(t) = 2i_{R4}$
 $= 2(i_{R2} - j(t))$

$$\begin{bmatrix} R_1 + R_2 & R_2 \\ R_2 & R_2 + R_3 + R_4 \end{bmatrix} \begin{bmatrix} i_{R1} \\ i_{R2} \end{bmatrix} + \begin{bmatrix} -1 \\ -1 \end{bmatrix} e(t) + \begin{bmatrix} 0 \\ -R_4 \end{bmatrix} j(t) + \begin{bmatrix} 0 \\ R_3 \end{bmatrix} j_b(t) = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

\downarrow
 $2i_{R4} = 2(i_{R2} - j(t))$

$$\begin{bmatrix} R_1 + R_2 & R_2 \\ R_2 & R_2 + 3R_3 + R_4 \end{bmatrix} \begin{bmatrix} i_{R1} \\ i_{R2} \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix} e(t) + \begin{bmatrix} 0 \\ 2R_3 + R_4 \end{bmatrix} j(t)$$

$$\begin{bmatrix} (2+4) & 4 \\ 4 & (4+9+5) \end{bmatrix} \begin{bmatrix} i_{R1} \\ i_{R2} \end{bmatrix} = \begin{bmatrix} 10 \\ 10 \end{bmatrix} + \begin{bmatrix} 0 \\ 11 \end{bmatrix} \cdot 2$$

$$\begin{bmatrix} 6 & 4 \\ 4 & 18 \end{bmatrix} \begin{bmatrix} i_{R1} \\ i_{R2} \end{bmatrix} = \begin{bmatrix} 10 \\ 32 \end{bmatrix} \Rightarrow i_{R1} = \frac{\begin{vmatrix} 10 & 4 \\ 32 & 18 \end{vmatrix}}{\begin{vmatrix} 6 & 4 \\ 4 & 18 \end{vmatrix}} = \frac{52}{92} \Rightarrow \boxed{i_{R1} = 0,565A}$$

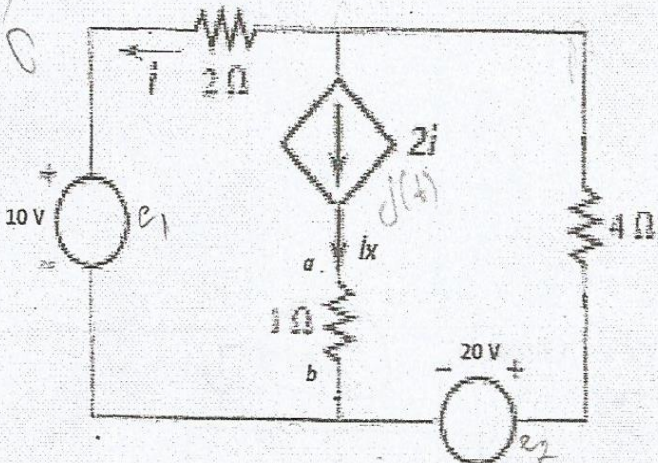
$$i_{R2} = \frac{\begin{vmatrix} 6 & 10 \\ 4 & 32 \end{vmatrix}}{\begin{vmatrix} 6 & 4 \\ 4 & 18 \end{vmatrix}} = \frac{152}{92} \Rightarrow \boxed{i_{R2} = 1,652A}$$

$$P_{R3} = R_3 i_{R3}^2 \Rightarrow i_{R3} = i_{R2} + j_b(t) = i_{R2} + 2i_{R4} = i_{R2} + 2(i_{R2} - j(t))$$

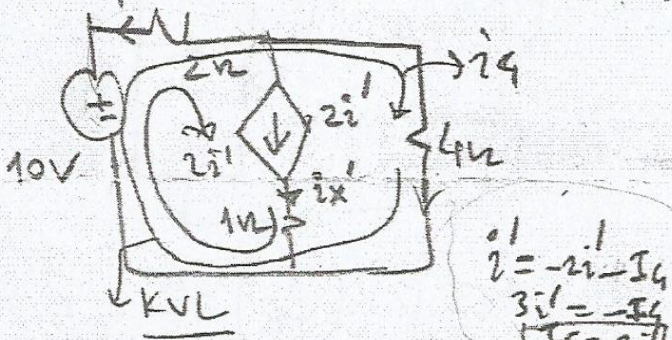
$$i_{R3} = 3i_{R2} - 2j(t) = 3 \cdot 1,652 - 2 \cdot 2 \Rightarrow \boxed{i_{R3} = 0,956A}$$

$$P_{R3} = R_3 i_{R3}^2 = 3 \cdot 0,956^2 \Rightarrow \boxed{P_{R3} = 2,742W}$$

Soru 1) Şekilde verilen devrede a-b arasındaki 1Ω 'luk direncin akımını (i_x) Süperpozisyon (toplamsallık) teoremini kullanarak bulunuz. (35 P)



10V varken (20V → k.D.)
($2i$ devrede)



$$4i_g - 10 + 2 \cdot (2i' + i_g) = 0$$

$$6i_g - 10 + 4i' = 0$$

$$6 \cdot (-3i') + 4i' = 10$$

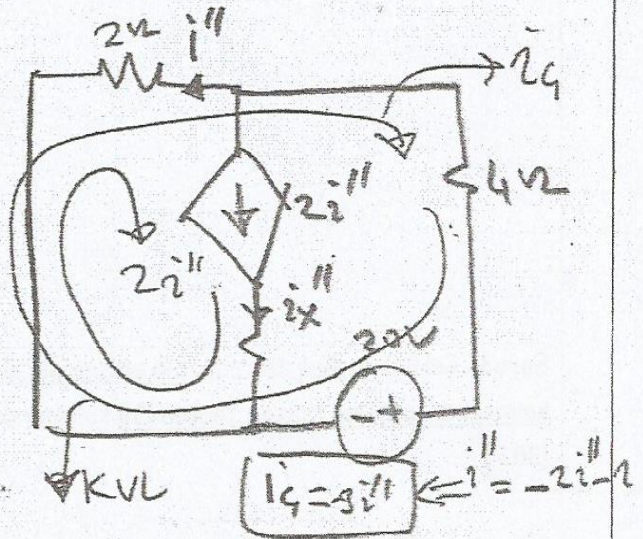
$$-14i' = 10 \Rightarrow i' = -\frac{5}{7} A$$

$$\begin{aligned} i' &= -2i' - I_g \\ 3i' &= -I_g \\ I_g &= -3i' \end{aligned}$$

$$i_x = -\frac{10}{7} A$$

Çözüm 1)

20V varken (10V → k.D.)
($2i$ devrede)



$$4i_g + 20 + 2 \cdot (2i'' + i_g) = 0$$

$$6i_g + 20 + 4i'' = 0$$

$$6 \cdot (-3i'') + 4i'' = -20$$

$$-14i'' = -20$$

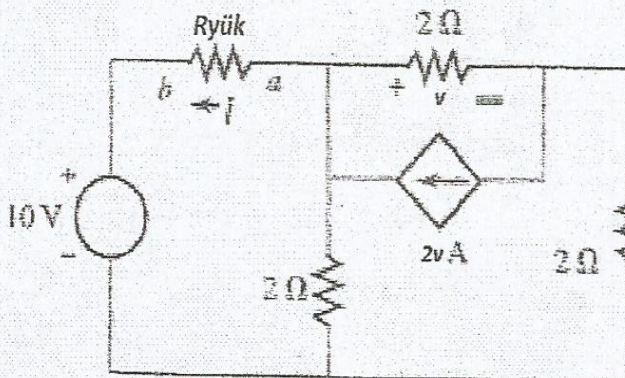
$$i'' = \frac{10}{7} A$$

$$i_x'' = \frac{20}{7} A$$

Sonuç olarak

$$i_x = i_x' + i_x'' = -\frac{10}{7} + \frac{20}{7} = \frac{10}{7} A$$

Soru 2) Şekilde verilen devrede a-b arasındaki yük direncine iletebilecek maksimum gücü bulunuz. (35 P)

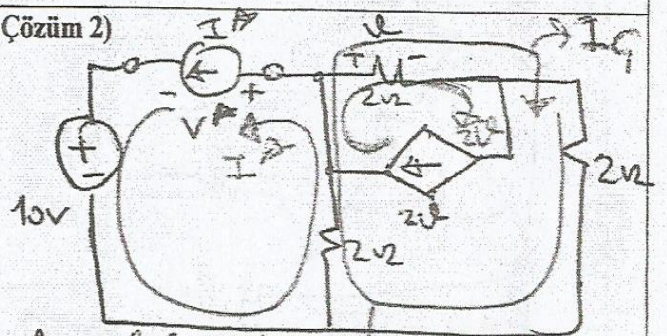


$$R_{th} = \frac{4}{3} \Omega \quad V_{th} = -10V$$

$$P_{max, R_{yuk}} = \frac{V_{th}^2}{4 \cdot R_{th}} = \frac{100}{4 \cdot (\frac{4}{3})}$$

$$P_{max, R_{yuk}} = \frac{500}{11} = 31,25W$$

Çözüm 2)



$$V = 2 \cdot (2I_g + I_g)$$

$$V = \frac{2}{3} I_g \quad I_g = (-\frac{3}{2} V)$$

$$2I_g + 2 \cdot (I_g + I^*) + 2 \cdot (I_g + 2V) = 0$$

$$6I_g + 4 \cdot (-\frac{2}{3} I_g) + 2I^* = 0$$

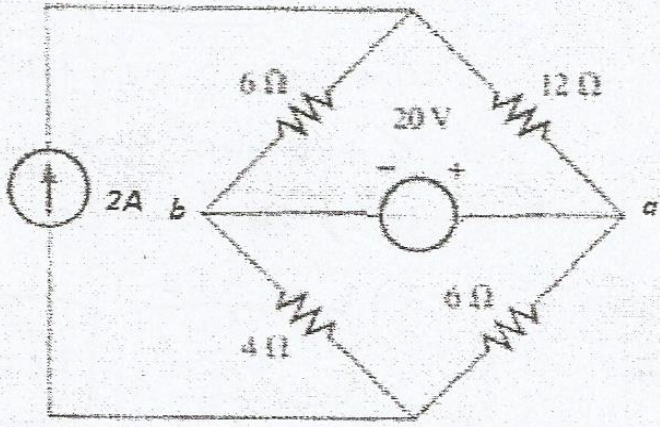
$$\frac{10}{3} I_g = -2I^* \Rightarrow I_g = -\frac{6}{10} I^*$$

$$I_g = -\frac{3}{5} I^*$$

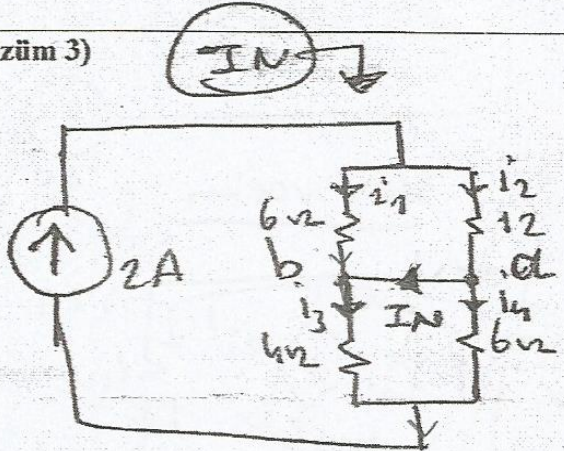
I^* için KVL

$$V^* + 10 + 2 \cdot (I^* - \frac{3}{5} I^*) = 0$$

Soru3) Şekilde verilen devrede, a-b arasındaki ~~altın~~ ~~gerilim~~ kaynağının gücünü, Norton Teoremi'ni kullanarak bulunuz. (30 P)



Çözüm 3)



$$i_1 = (2) \cdot \left(\frac{12}{18}\right) = \frac{24}{18} = \frac{4}{3} \text{ A}$$

$$i_2 = (2) \cdot \left(\frac{6}{18}\right) = \frac{12}{18} = \frac{2}{3} \text{ A}$$

$$i_3 = (2) \cdot \left(\frac{6}{10}\right) = \frac{12}{10} = \frac{6}{5} \text{ A}$$

$$i_4 = (2) \cdot \left(\frac{4}{10}\right) = \frac{8}{10} = \frac{4}{5} \text{ A}$$

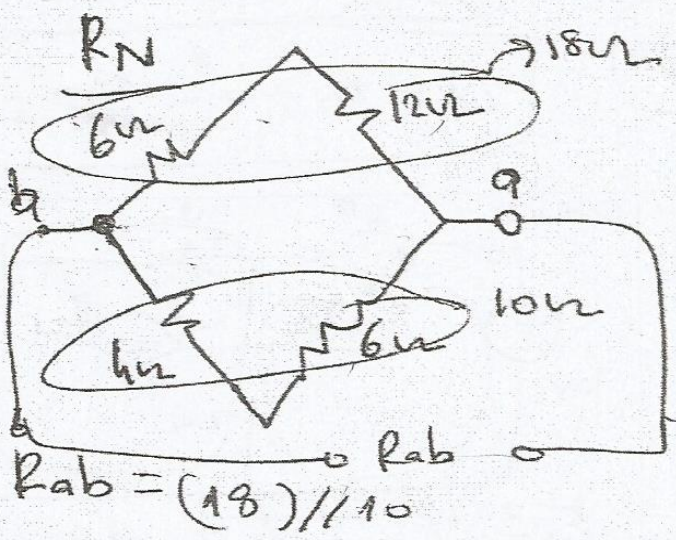
a → KCL

$$I_2 = I_N + I_4$$

$$I_N = I_2 - I_4$$

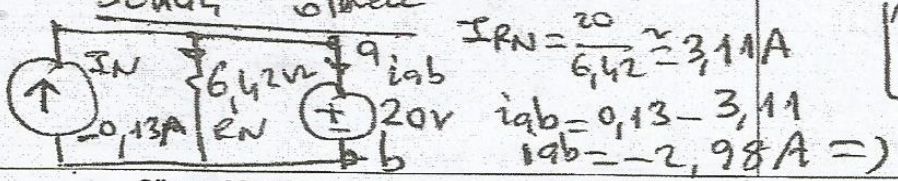
$$I_N = \frac{2}{3} - \frac{4}{5} = \frac{-2}{15} \text{ A}$$

$$I_N \approx -0,13 \text{ A}$$



$$R_{ab} = (18) // 10$$

$$R_{ab} = \frac{18 \cdot 10}{28} = \frac{180}{28} \approx 6,42 \Omega$$



$$I_{RN} = \frac{20}{6,42} \approx 3,11 \text{ A}$$

$$i_{ab} = 0,13 - 3,11$$

$$i_{ab} = -2,98 \text{ A} \Rightarrow$$